

# Correction to “Elastic wave speeds and moduli in polycrystalline ice Ih, sI methane hydrate, and sII methane-ethane hydrate”

M. B. Helgerud, W. F. Waite, S. H. Kirby, and A. Nur

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[1] In the paper “Elastic wave speeds and moduli in polycrystalline ice Ih, sI methane hydrate, and sII methane-ethane hydrate” by M. B. Helgerud, W. F. Waite, S. H. Kirby, and A. Nur (*Journal of Geophysical Research*, **114**, B02212, doi:10.1029/2008JB006132, 2009), the mathematical formula listed in Tables 1–3, and A1 is incorrect. The correct headings are given here.

**Table 1.** Regressions of  $V_p$  and  $V_s$ ,  $\nu$ , and  $M$ ,  $G$ , and  $K$  Versus Temperature and Piston Pressure for Compacted, Polycrystalline Ice Ih<sup>a</sup>

	$F(T,P) = aT + bP + c$			
	$a^b$	$b^b$	$c^b$	Uncertainty <sup>c</sup>
$V_p$ (m s <sup>-1</sup> )	$-2.67 \pm 0.05$	$0.2 \pm 0.08$	$3864 \pm 2$	$\pm 1.5$
$V_s$ (m s <sup>-1</sup> )	$-1.244 \pm 0.005$	$-0.198 \pm 0.007$	$1942.4 \pm 0.2$	$\pm 1.5$
$\nu$	$-(2.0 \pm 0.6) \times 10^{-5}$	$(6.8 \pm 0.9) \times 10^{-5}$	$0.3310 \pm 0.0002$	$\pm 3$
$M$ (GPa)	$-(2.15 \pm 0.04) \times 10^{-2}$	$(4.02 \pm 0.03) \times 10^{-3}$	$13.69 \pm 0.02$	$\pm 4$
$G$ (GPa)	$-(5.03 \pm 0.02) \times 10^{-3}$	$-(3.0 \pm 0.2) \times 10^{-4}$	$3.459 \pm 0.0007$	$\pm 4$
$K$ (GPa)	$-(1.48 \pm 0.04) \times 10^{-2}$	$(3.4 \pm 0.5) \times 10^{-3}$	$9.07 \pm 0.02$	$\pm 6$

<sup>a</sup> $V_p$ , compressional wave speeds;  $V_s$ , shear wave speeds;  $\nu$ , Poisson’s ratio;  $M$ , dynamic compressional wave;  $G$ , shear moduli; and  $K$ , bulk moduli; temperature of  $-20$  to  $-5^\circ\text{C}$ ; and piston pressure of  $22.4$  to  $32.8$  MPa. Calculated density range was  $0.920$  to  $0.923$  g cm<sup>-3</sup>.

<sup>b</sup>Units for  $a$  are the units of the property being fit divided by  $^\circ\text{C}$ . Units for  $b$  are those of the property being fit divided by MPa. Units for  $c$  are those of the property being fit.

<sup>c</sup>Uncertainty is given as a percentage of the property being fit.

**Table 2.** Regressions of  $V_p$  and  $V_s$ ,  $\nu$ , and  $M$ ,  $G$ , and  $K$  Versus Temperature and Piston Pressure for Compacted, sI Methane Hydrate<sup>a</sup>

	$F(T,P) = aT + bP + c$			
	$a^b$	$b^b$	$c^b$	Uncertainty <sup>c</sup>
$V_p$ (m s <sup>-1</sup> )	$-1.84 \pm 0.03$	$0.31 \pm 0.02$	$3766 \pm 2$	$\pm 1.5$
$V_s$ (m s <sup>-1</sup> )	$-0.892 \pm 0.005$	$-0.100 \pm 0.003$	$1957.0 \pm 0.2$	$\pm 1.5$
$\nu$	$-(9 \pm 4) \times 10^{-5}$	$(6.6 \pm 0.3) \times 10^{-5}$	$0.3151 \pm 0.0002$	$\pm 3$
$M$ (GPa)	$-(1.64 \pm 0.02) \times 10^{-2}$	$(4.02 \pm 0.03) \times 10^{-3}$	$13.11 \pm 0.01$	$\pm 4$
$G$ (GPa)	$-(4.2 \pm 0.02) \times 10^{-3}$	$(9 \pm 1) \times 10^{-5}$	$3.541 \pm 0.0008$	$\pm 4$
$K$ (GPa)	$-(1.09 \pm 0.02) \times 10^{-2}$	$(3.8 \pm 0.2) \times 10^{-3}$	$8.39 \pm 0.01$	$\pm 6$

<sup>a</sup>Same as Table 1 except temperature of  $-20$  to  $15^\circ\text{C}$  and piston pressure of  $30.5$  to  $97.7$  MPa. Calculated density range was  $0.924$  to  $0.933$  g cm<sup>-3</sup>.

<sup>b</sup>Units for  $a$  are the units of the property being fit divided by  $^\circ\text{C}$ . Units for  $b$  are those of the property being fit divided by MPa. Units for  $c$  are those of the property being fit.

<sup>c</sup>Uncertainty is given as a percentage of the property being fit.

**Table 3.** Regressions of  $V_p$  and  $V_s$ ,  $\nu$ , and  $M$ ,  $G$ , and  $K$  Versus Temperature and Piston Pressure for Compacted, Polycrystalline sII Methane-Ethane Hydrate<sup>a</sup>

	$F(T,P) = aT + bP + c$			Uncertainty <sup>c</sup>
	$a^b$	$b^b$	$c^b$	
$V_p$ (m s <sup>-1</sup> )	$-1.825 \pm 0.008$	$(3.10 \pm 0.05) \times 10^{-1}$	$3821.8 \pm 0.3$	1.5
$V_s$ (m s <sup>-1</sup> )	$-0.894 \pm 0.002$	$-(0.87 \pm 0.01) \times 10^{-1}$	$2001.14 \pm 0.08$	1.5
$\nu$	$-(1.4 \pm 0.1) \times 10^{-5}$	$(6.29 \pm 0.07) \times 10^{-5}$	$0.31119 \pm 0.00004$	3
$M$ (GPa)	$-(1.564 \pm 0.005) \times 10^{-2}$	$(4.02 \pm 0.03) \times 10^{-3}$	$13.407 \pm 0.002$	4
$G$ (GPa)	$-(4.021 \pm 0.007) \times 10^{-3}$	$(1.66 \pm 0.04) \times 10^{-4}$	$3.6764 \pm 0.0003$	4
$K$ (GPa)	$-(1.028 \pm 0.005) \times 10^{-2}$	$(3.80 \pm 0.03) \times 10^{-3}$	$8.505 \pm 0.002$	6

<sup>a</sup>Same as Table 1 except temperature of  $-20$  to  $10^\circ\text{C}$  and piston pressure of  $30.5$  to  $91.6$  MPa. Sample density calculated theoretically as a function of temperature and pressure with 94% cage occupancy, 79.25% methane, 20.75% ethane. Calculated density range was  $0.917$  to  $0.931$  g cm<sup>-3</sup>.

<sup>b</sup>Units for  $a$  are the units of the property being fit divided by  $^\circ\text{C}$ . Units for  $b$  are those of the property being fit divided by MPa. Units for  $c$  are those of the property being fit.

<sup>c</sup>Uncertainty is given as a percentage of the property being fit.

**Table A1.** Regressions of Density Versus Temperature for Solid Ice Ih, sI Methane Hydrate, and sII Methane-Ethane Hydrate<sup>a</sup>

Material	$\rho(T,P) = aT + bP + c$			Uncertainty <sup>c</sup>
	$a^b$	$b^b$	$c^b$	
Ice Ih	$-1.5035 \times 10^{-4}$	$1.0594 \times 10^{-4}$	$0.91673$	3
sI methane hydrate	$-2.3815 \times 10^{-4}$	$1.1843 \times 10^{-4}$	$0.92435$	3
sII methane-ethane hydrate	$-1.7719 \times 10^{-4}$	$1.2228 \times 10^{-4}$	$0.91801$	3

<sup>a</sup>Both hydrate structures are assumed to have 94% cage occupancy. The ratio of methane to ethane in the sII hydrate is assumed to be 4:1. Temperature and pressure ranges are given in Tables 1–3.

<sup>b</sup>Units for  $a$  are the units of the property being fit divided by  $^\circ\text{C}$ . Units for  $b$  are those of the property being fit divided by MPa. Units for  $c$  are those of the property being fit.

<sup>c</sup>Uncertainty is given as a percentage of the property being fit.